

# **Atmospheric Passive Remote Sensing**

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# What is Passive Remote Sensing?



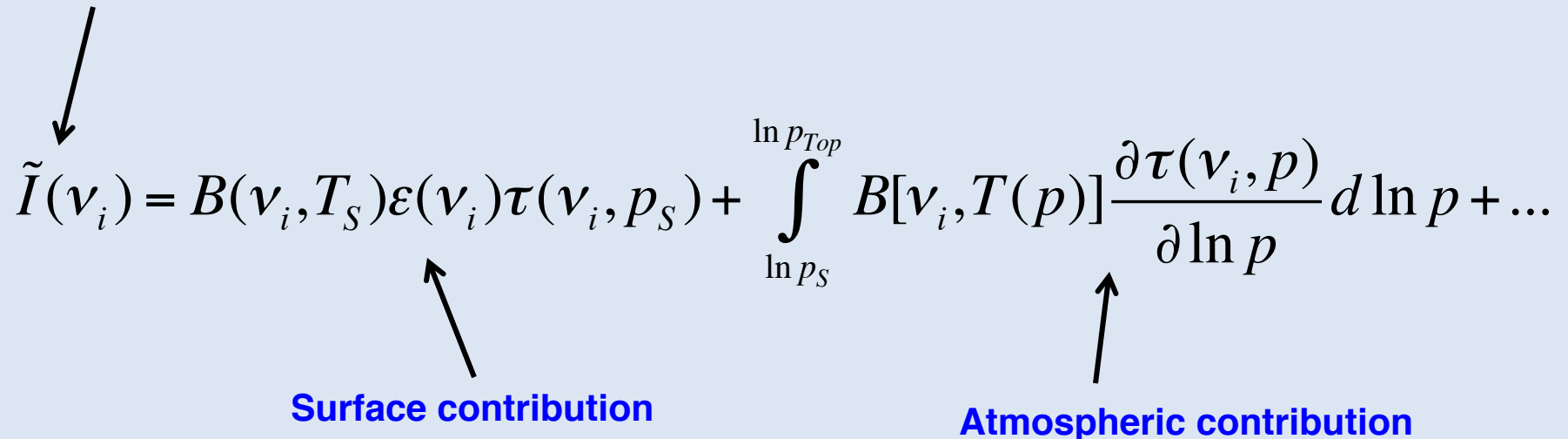
# Really, what is passive remote sensing?

- Remotely measured electromagnetic radiation where
  - the source is not controlled.
- Examples:
  - Visible and infrared imaging.
  - Backscattered solar ultraviolet.
  - Microwave and infrared emission spectra.
  - Solar occultation spectra.
- Two general types of space-based remote sensing:
  - Nadir (downward looking).
  - Limb-viewing.
- *Atmospheric remote sensing often means inferring vertical structure, called 'remote sounding'.*

# The Fundamental Approach: Use the Radiative Transfer Equation to Understand the Atmosphere

- We know *observed* radiance.
- We *want* internal information like  $T_s$ ,  $T(p)$ , etc.

Observed outgoing radiance



The diagram illustrates the components of the radiative transfer equation. A red label 'Observed outgoing radiance' has an arrow pointing to the left-hand side of the equation,  $\tilde{I}(\nu_i)$ . A blue label 'Surface contribution' has an arrow pointing to the first term on the right-hand side,  $B(\nu_i, T_s)\epsilon(\nu_i)\tau(\nu_i, p_s)$ . Another blue label 'Atmospheric contribution' has an arrow pointing to the integral term on the right-hand side,  $\int_{\ln p_s}^{\ln p_{Top}} B[\nu_i, T(p)] \frac{\partial \tau(\nu_i, p)}{\partial \ln p} d \ln p + \dots$ .

$$\tilde{I}(\nu_i) = B(\nu_i, T_s)\epsilon(\nu_i)\tau(\nu_i, p_s) + \int_{\ln p_s}^{\ln p_{Top}} B[\nu_i, T(p)] \frac{\partial \tau(\nu_i, p)}{\partial \ln p} d \ln p + \dots$$

# Two Basic Aspects of Remote Sounding

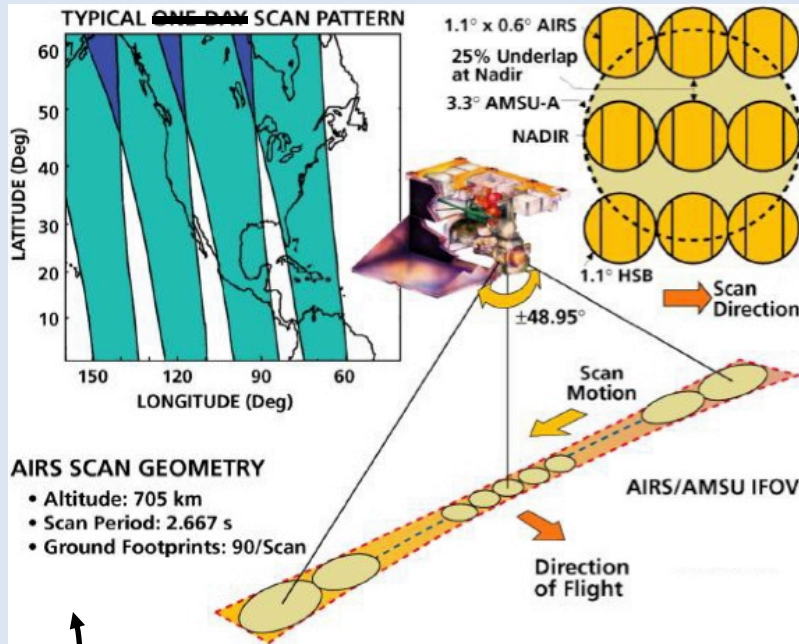
1. *The forward problem:* given a known internal state (surface, atmosphere, clouds), what is the emitted radiance?
2. *The retrieval or inverse problem:* what internal state explains observed radiances? (Impossible without a forward model.)

Inverse problems are found in many branches of geophysics, astrophysics, and medicine. Most infer physical state from propagating waves.

# A Nadir Sounding Example: The AIRS/AMSU Suite

AIRS = Atmospheric Infrared Sounder

AMSU = Advanced Microwave Sounding Unit



1. AMSU footprint, 45 km across at nadir, contains 9 AIRS spectra

– THIS IS THE RETRIEVAL GRANULARITY.

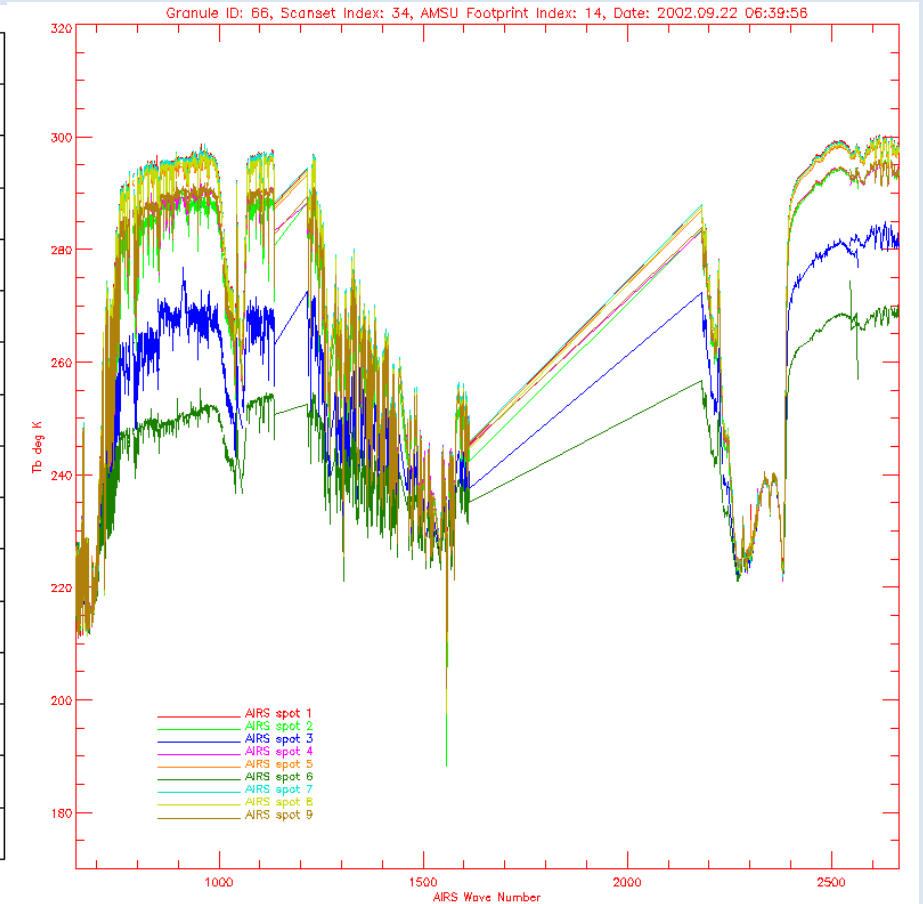
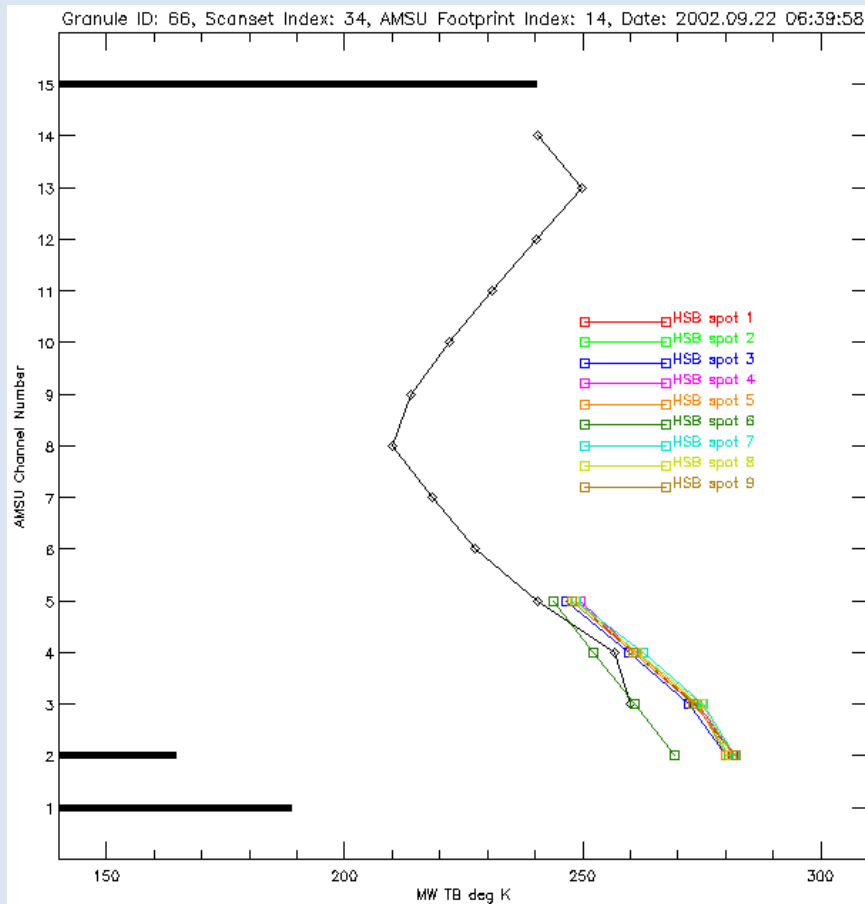
2. Viewing swath 30 AMSU footprints or ~1650 km wide.

3. The result: 324,000 retrievals per day (over a 15 year record).

# One Set of AIRS Suite Spectra in the Atlantic

We now have about  $10^9$  in a sixteen year record  
(about  $10^{10}$  IR spectra)

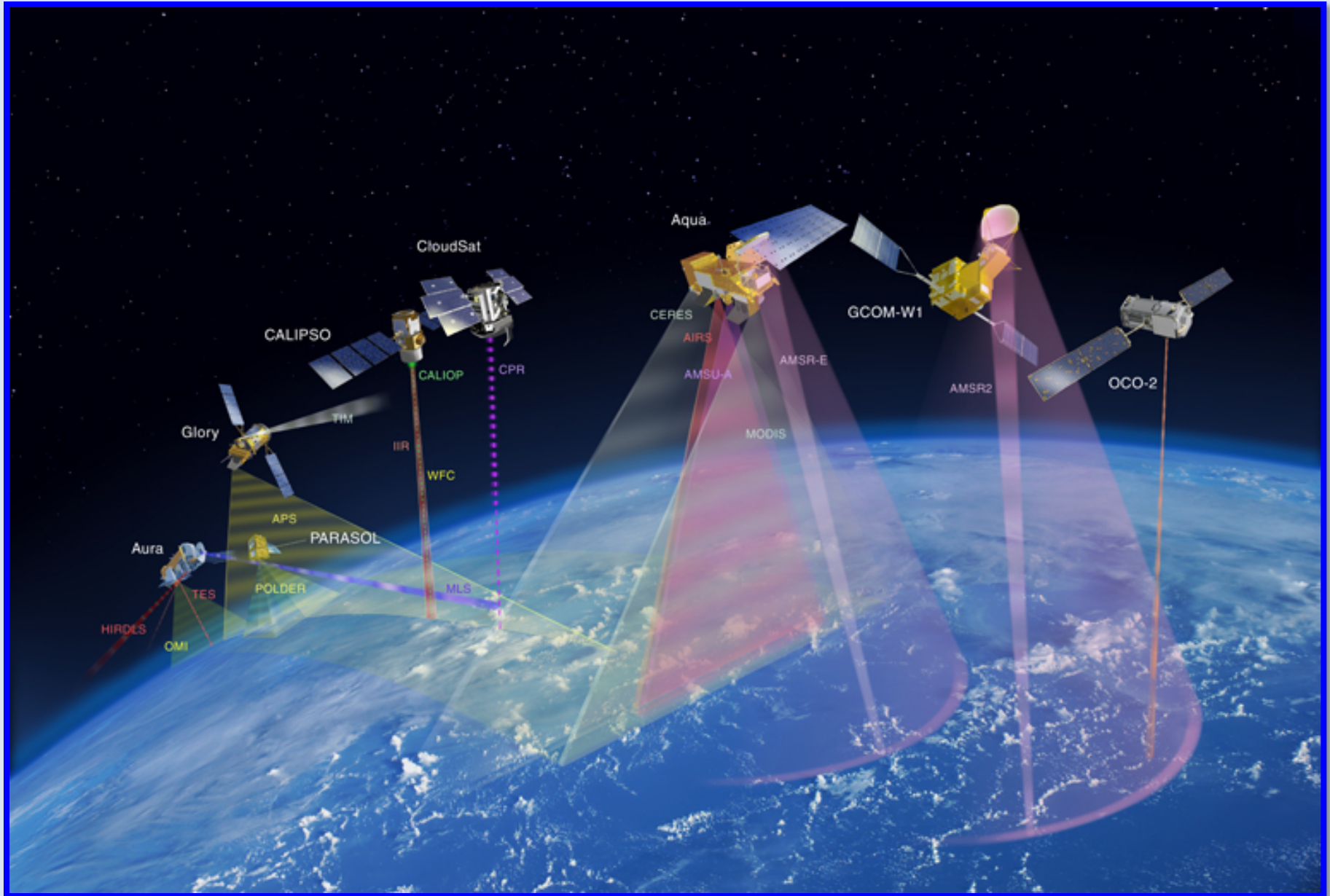
22 Sep 2002, 0630 UT, night time near 25 N and 73 W



1 AMSU, 9 HSB Spectra

9 AIRS Spectra

# AIRS is One Example from the A-Train: An international commitment to climate science



# About Retrieved Quantities

*Retrieved quantities are inferences (estimates) of the true state of the atmosphere.*

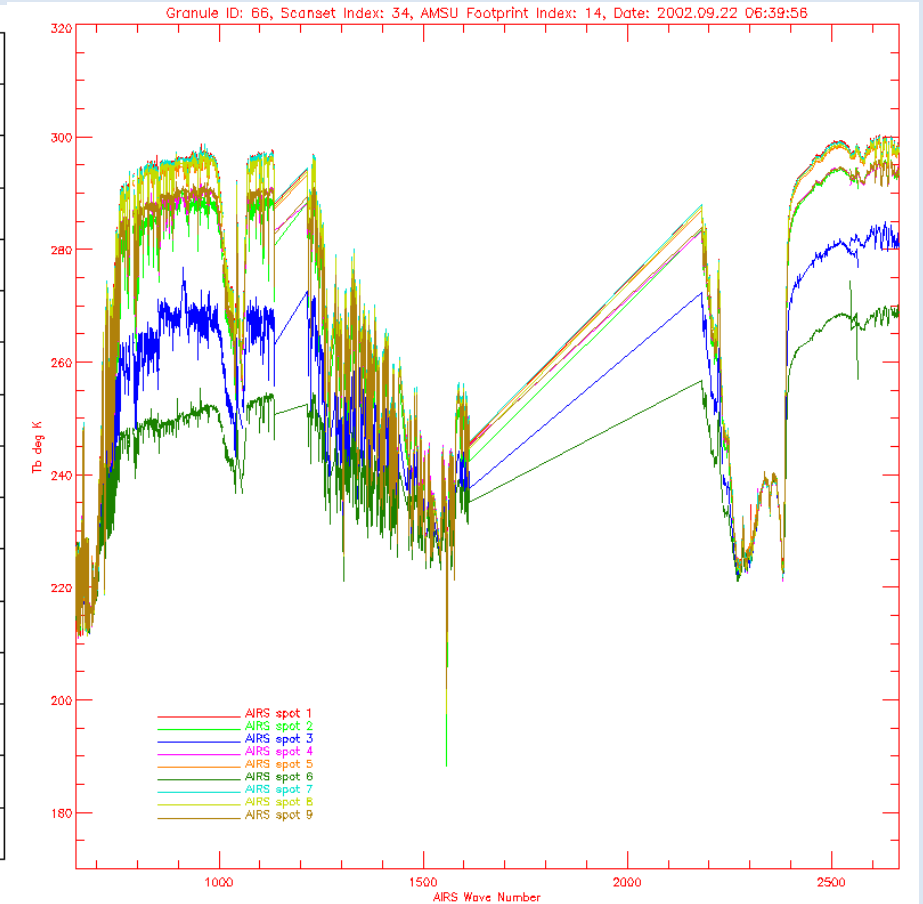
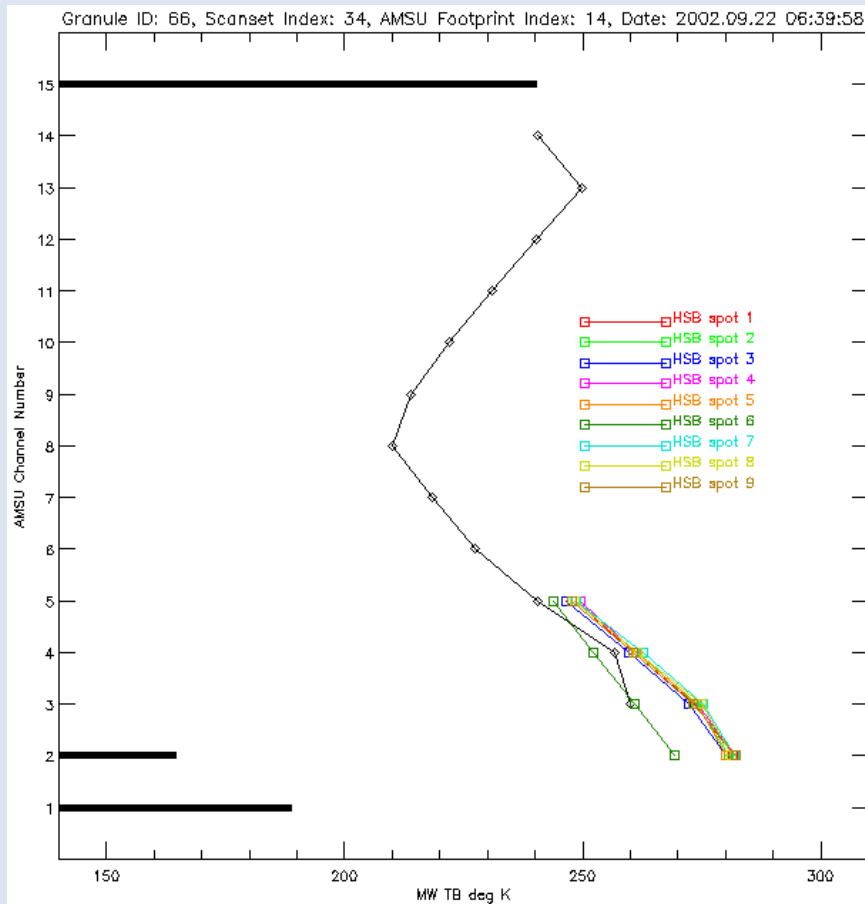
Some basic challenges:

1. Developing a reliable forward model.
  - This usually means detailed spectroscopic knowledge.
2. Implementing a retrieval algorithm.
3. ‘Validation’ of retrievals against other measurements.
4. Interpretation of resulting very large data sets.

# One Set of AIRS Suite Spectra in the Atlantic

We now have about  $10^9$  in a sixteen year record  
(about  $10^{10}$  IR spectra)

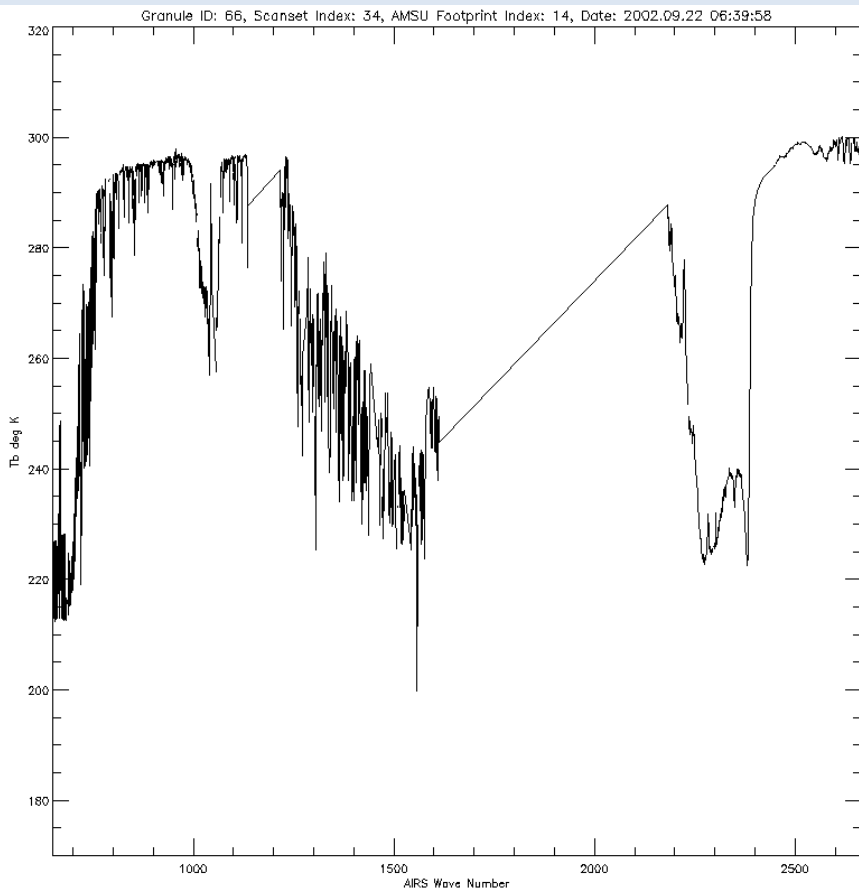
22 Sep 2002, 0630 UT, night time near 25 N and 73 W



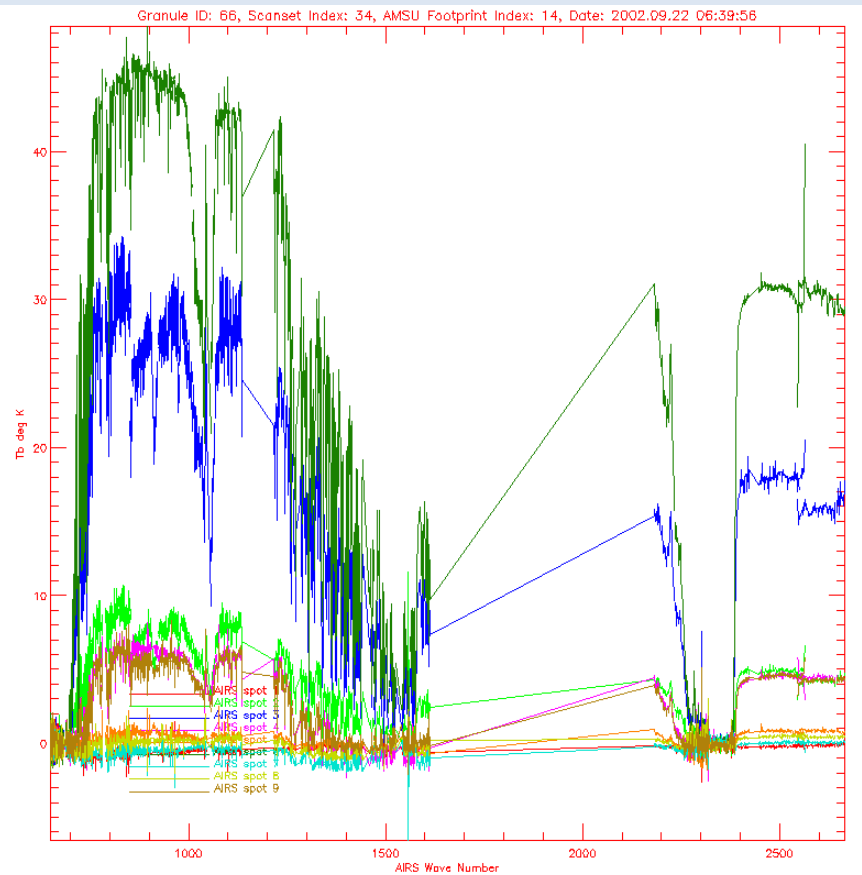
1 AMSU, 9 HSB Spectra

9 AIRS Spectra

# ***Retrieved Cloud-Cleared Spectrum*** and differences from radiances in previous slide



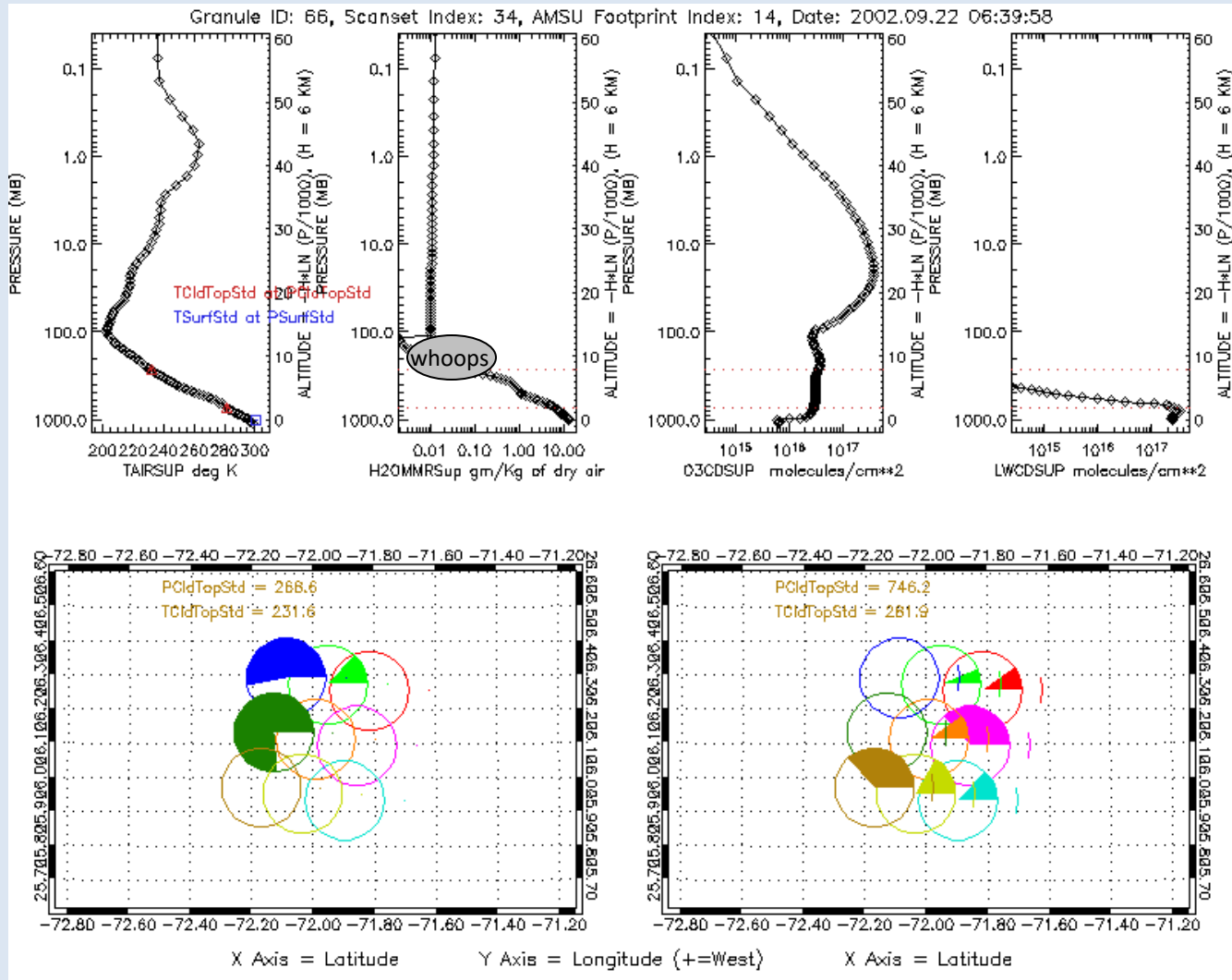
**1 Cloud-Cleared Spectrum**



**CC Spectrum – 9 AIRS Spectra**

# Retrieved Geophysical Quantities

(from the cloud cleared radiances just shown)



# The Radiative Transfer Equation and Weighting Functions

**Weighting functions relate internal state and calculated outgoing radiance**



**Observed radiance**

$$\tilde{I}(\nu_i) = B(\nu_i, T_S) \varepsilon(\nu_i) \tau(\nu_i, p_S) + \int_{\ln p_S}^{\ln p_{Top}} B[\nu_i, T(p)] \frac{\partial \tau(\nu_i, p)}{\partial \ln p} d \ln p + \dots$$

**Surface contribution**

**Atmospheric contribution**

# Nadir Weighting Functions

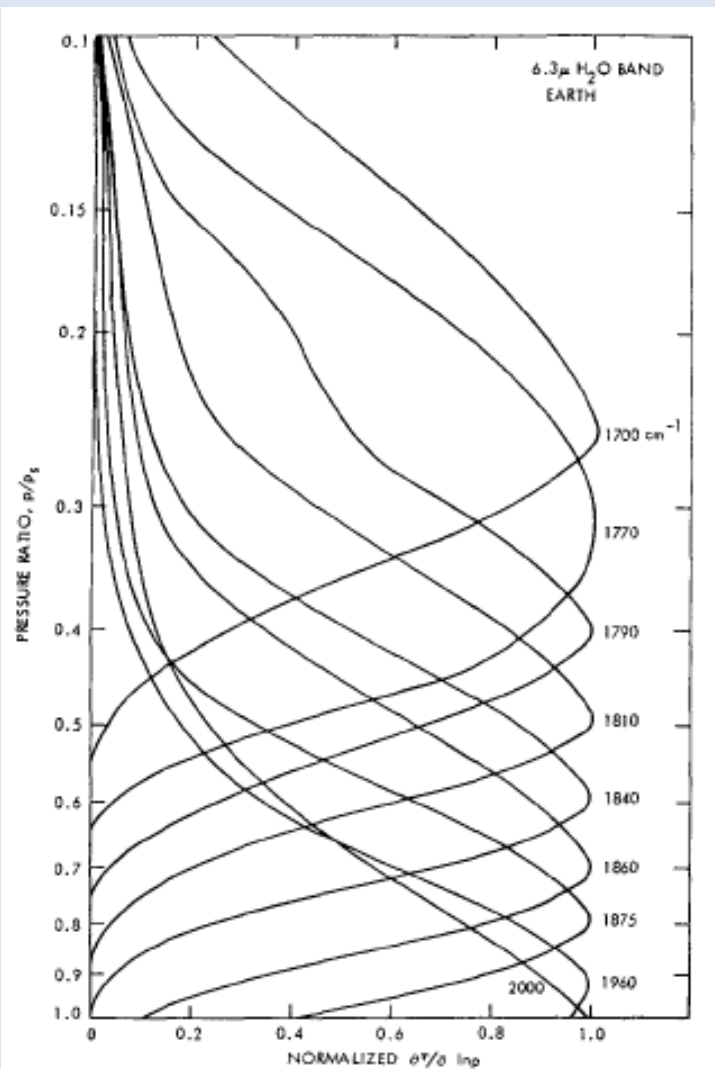


FIG. 1. Normalized weighting functions ( $d\tau/d \ln p$ ) for the selected set of nine sounding frequencies computed for an instrumental slit function of  $5 \text{ cm}^{-1}$  (see text).

$$\frac{\partial \tau(\nu_i, p)}{\partial \ln p}$$

**Weighting Function =  
Vertical Derivative of  
Optical Depth**

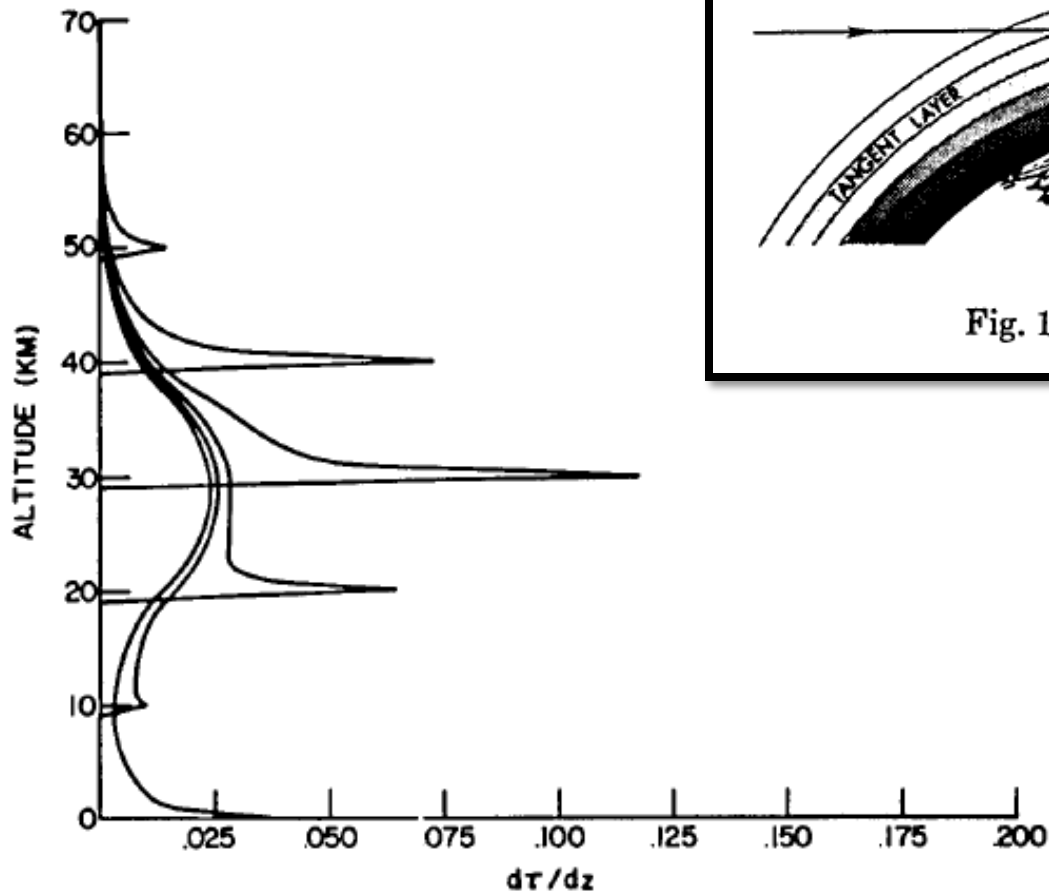
The functions show the contribution an altitude makes to calculated radiance.

Also called:

- Adjoints
- Jacobians

**Note: Fine scale structure is retrieved by deconvolving weighting functions.**

# Limb Viewing Geometry and Weighting Functions



2. Limb experiment vertical ozone weighting functions in the 9.6- $\mu\text{m}$  band at selected tangent heights.

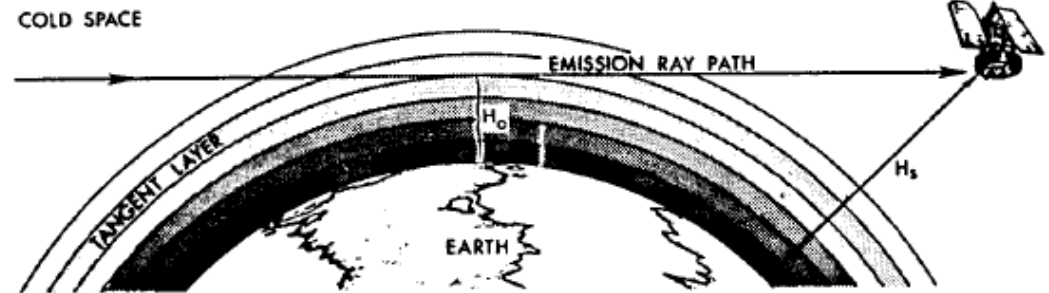


Fig. 1. Limb experiment geometry.

*From Gordley and Russell, 1981, Applied Optics.*

# Limb Viewing Characteristics

## Good:

- The limb is viewed against cold space
  - high signal-to-noise
  - no surface term in the retrieval.
- Very sharp weighting functions
  - give high vertical resolution.

## Not so good:

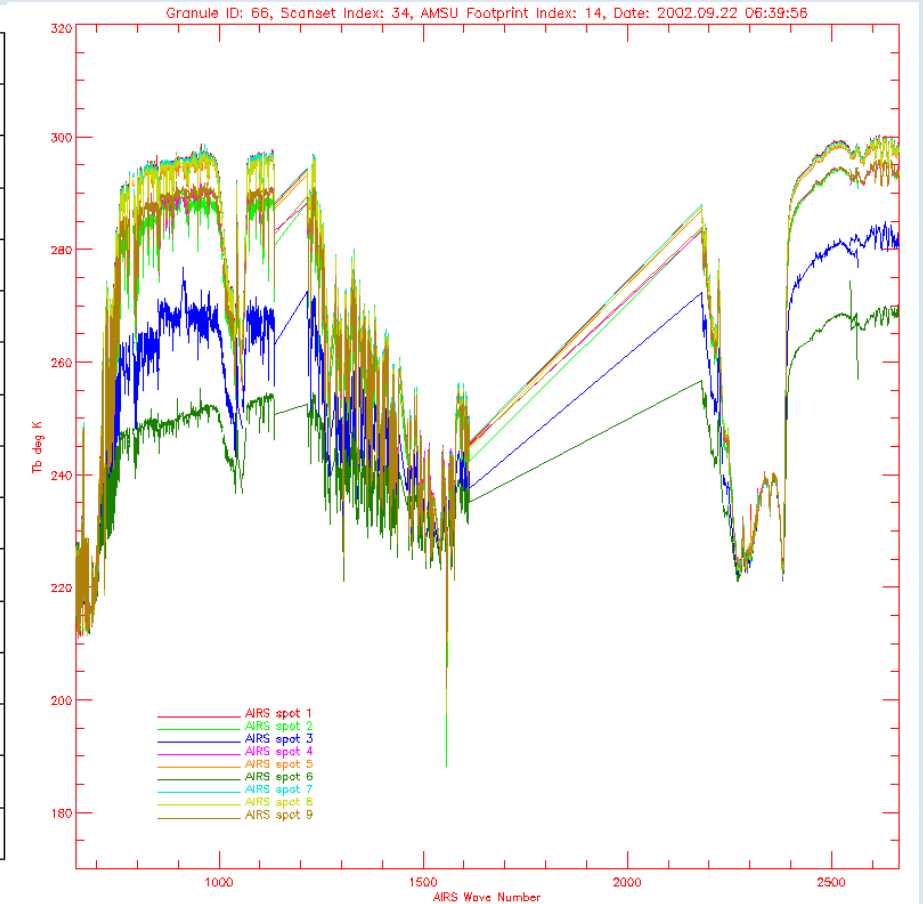
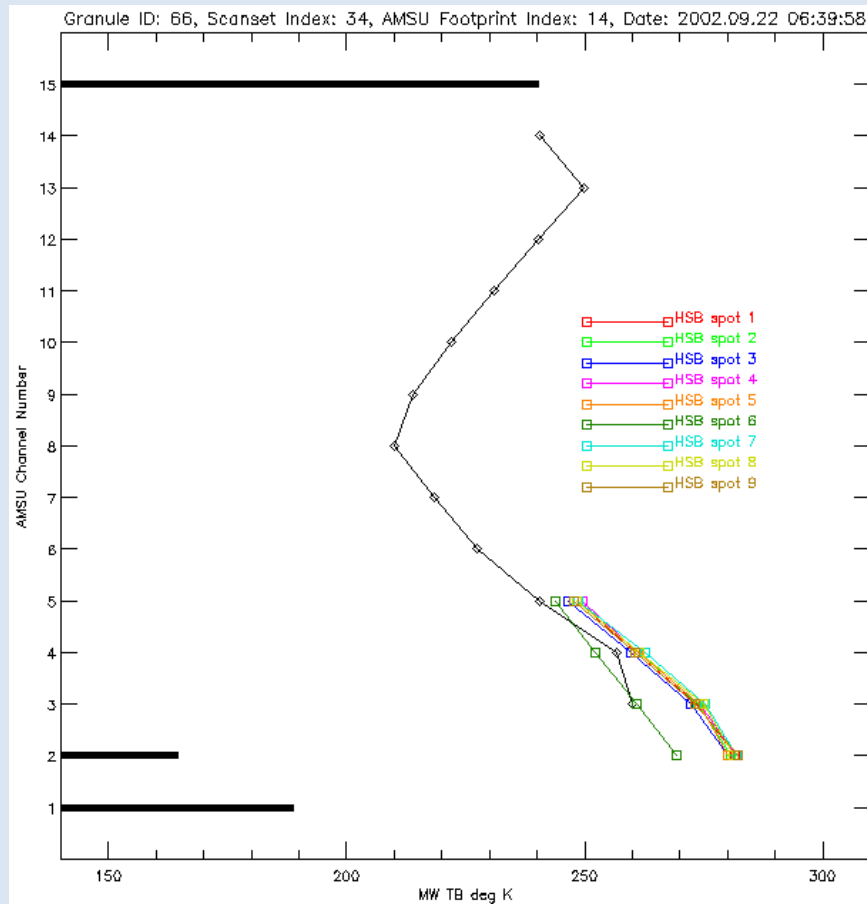
- Very sensitive to clouds.
  - Makes limb sounding most useful in middle troposphere and up.

**Note:** GPS limb occultations can be inverted to stable, very high resolution, cloud-free profiles. *But, not a passive technique, also temperature-water vapor ambiguity for  $T > 250$  K.*

# How Much Information?

## Retrieval algorithms extract the information content of spectra.

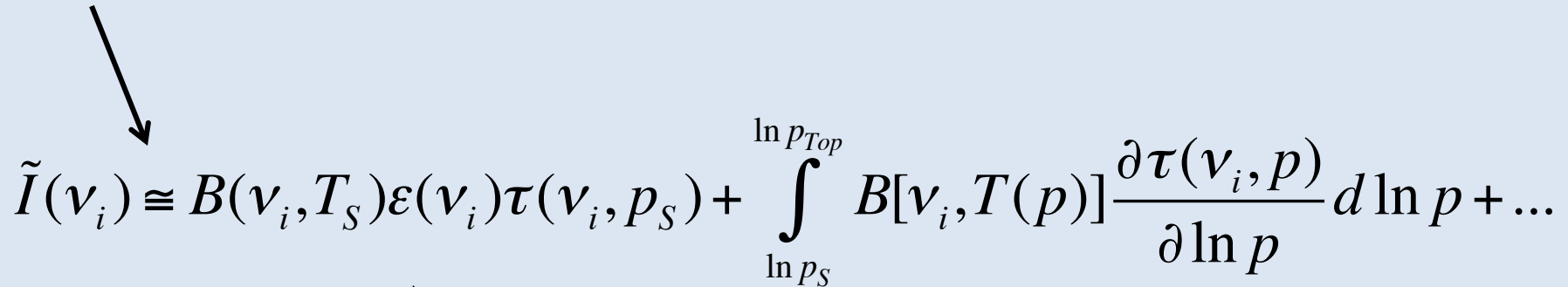
22 Sep 2002, 0630 UT, night time near 25 N and 73 W



# *An Admission:*

This ‘equation’ is not an equation.

**Observed** radiance



The diagram shows the equation for observed radiance,  $\tilde{I}(\nu_i) \cong B(\nu_i, T_S) \epsilon(\nu_i) \tau(\nu_i, p_S) + \int_{\ln p_S}^{\ln p_{Top}} B[\nu_i, T(p)] \frac{\partial \tau(\nu_i, p)}{\partial \ln p} d \ln p + \dots$ . An arrow points from the text 'Observed radiance' to the left-hand side of the equation. Another arrow points from the text 'Calculated surface contribution' to the first term of the equation. A third arrow points from the text 'Calculated atmospheric contribution' to the integral term of the equation.

$$\tilde{I}(\nu_i) \cong B(\nu_i, T_S) \epsilon(\nu_i) \tau(\nu_i, p_S) + \int_{\ln p_S}^{\ln p_{Top}} B[\nu_i, T(p)] \frac{\partial \tau(\nu_i, p)}{\partial \ln p} d \ln p + \dots$$

**Calculated** surface contribution

**Calculated** atmospheric contribution

# Retrieving internal parameters is a *minimization* problem.

- We know *observed* radiance
- Match these with *hypothesized* internal information like  $T_s$ ,  $T(p)$ , etc.
  - Calculation requires a forward model.
  - Need to choose a cost function for the minimization, as here:

**Observed** radiance

$$\varepsilon = \min \left\| \tilde{I}(\nu_i) - B(\nu_i, T_s) \varepsilon(\nu_i) \tau(\nu_i, p_s) - \int_{\ln p_s}^{\ln p_{Top}} B[\nu_i, T(p)] \frac{\partial \tau(\nu_i, p)}{\partial \ln p} d \ln p \right\|$$

**Calculated** surface contribution

**Calculated** atmospheric contribution

# **One Approach: Statistical Retrievals**

**Tabulate simulated radiances for a wide range of conditions,  
then regress the observed radiances onto known states.**

- **Advantages**
  - **Fast.**
  - **Simple.**
- **Disadvantages**
  - **Weak mathematical or physical justification.**
  - **Poor uncertainty propagation.**

# Another Approach: Physical Relaxation

Iterate this equation until  $\varepsilon$  is within acceptable limits.

$$\varepsilon = \min \left\| \tilde{I}(v_i) - B(v_i, T_S) \varepsilon(v_i, p_S) - \int_{\ln p_S}^{\ln p_{Top}} B[v_i, T(p)] \frac{\partial \tau(v_i, p)}{\partial \ln p} d \ln p \right\|$$

- **Advantages:**
  - Some physical justification
  - Computationally fast.
- **Disadvantages**
  - Physical justification is ad hoc.
  - Solution may have multiple minima.
  - Poor uncertainty propagation.

# **Yet Another Approach: Optimal Estimation (Bayesian) Methods**

- **Advantages:**
  - **Good mathematical foundation.**
  - **Incorporates prior information; explicitly handles error propagation and multiple minima.**
- **Disadvantages**
  - **Computationally expensive.**
  - **Require prior information, including a climatology.**
  - **‘Some people treat it like a religion.’ -Anonymous JPLer**

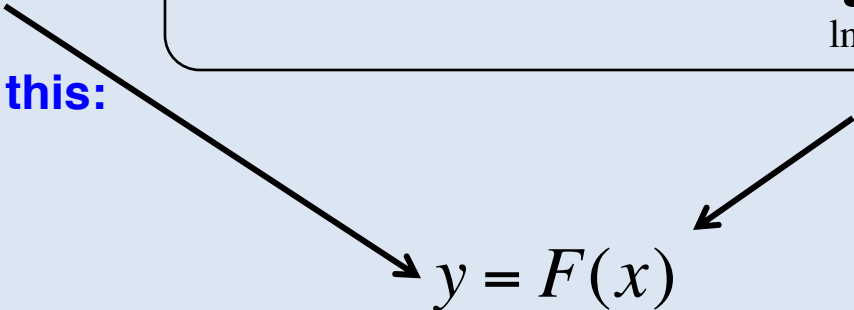
**Optimal estimation is becoming the community standard, though not all instruments use it (e. g. AIRS currently uses a combined statistical and relaxation method).**

# Optimal Estimation: Generalize the Inverse Problem

Reduce this:

$$\tilde{I}(\nu_i) \cong B(\nu_i, T_S) \varepsilon(\nu_i) \tau(\nu_i, p_S) + \int_{\ln p_S}^{\ln p_{Top}} B[\nu_i, T(p)] \frac{\partial \tau(\nu_i, p)}{\partial \ln p} d \ln p$$

to this:


$$y = F(x)$$

Where

$x$  = vector of retrieved quantities [ $T_s$ ,  $T(p)$ , etc.].

$y$  = vector of observed radiances.

$F$  = forward (radiance) model.

We want the inverse:

$$x = F^{-1}(y)$$

# Optimal Estimation in a nutshell

**Minimize this cost function:**

$$\varepsilon = \min_x \left( \|y - F(x)\|_{S_n^{-1}}^2 + \|x - x_c\|_{\Lambda}^2 \right)$$

*Where*

$x$  = retrieved state vector

$y$  = observed radiance

$F(x)$  = forward modeled radiance

$S_n^{-1}$  = noise covariance matrix

$x_c$  = first guess

$\Lambda$  = constraint matrix.

**Slide courtesy Bill Irion, JPL**

# *An Aside*

- The cost function is a matter of taste.
- Two examples shown today:

$$\varepsilon = \min \left\| \tilde{I}(\nu_i) - B(\nu_i, T_S) \varepsilon(\nu_i) \tau(\nu_i, p_S) - \int_{\ln p_S}^{\ln p_{Top}} B[\nu_i, T(p)] \frac{\partial \tau(\nu_i, p)}{\partial \ln p} d \ln p \right\|$$

$$\varepsilon = \min_x \left( \|y - F(x)\|_{S_n^{-1}}^2 + \|x - x_c\|_{\Lambda}^2 \right)$$

- This is analogous to a choice of statistical characterization
  - Mean, mode, or median?
  - Standard deviation or interquartile range?
  - Chocolate or vanilla?
  - ...

# Jacobians (Weighting Functions) and Gain

**Jacobian** - relates change in forward model  $F$  to change in “true” state,  $x$ .

$$K = \frac{\partial F}{\partial x} \text{ same as } \frac{\partial \tau(\nu_i, p)}{\partial \ln p}$$

**Gain** - relates change in retrieved state,  $\hat{x}$ , to forward model radiance,  $F$ .

$S_n$  is the noise term  $[nn^T]$ , and  $\Lambda$  is the constraint matrix (usually prior covariance<sup>-1</sup>).

$$G = \frac{\partial \hat{x}}{\partial F} = \left( K^T S_n^{-1} K + \Lambda \right)^{-1} K^T S_n^{-1}$$

# Averaging Kernels and Information Content

Averaging kernel - relates change in retrieved state,  $\hat{x}$ , to true state,  $x$ .

$$A = \frac{\partial \hat{x}}{\partial x} = \frac{\partial \hat{x}}{\partial F} \frac{\partial F}{\partial x} = GK$$

Final retrieval, from the averaging kernel, smooths the difference between the true state,  $x$ , and the a priori,  $x_a$ .

$$\hat{x} = x_a + A(x - x_a) + Gn$$

***The trace of the averaging kernel matrix is the number of degrees of freedom in the retrieval.***

# AIRS Averaging Kernels

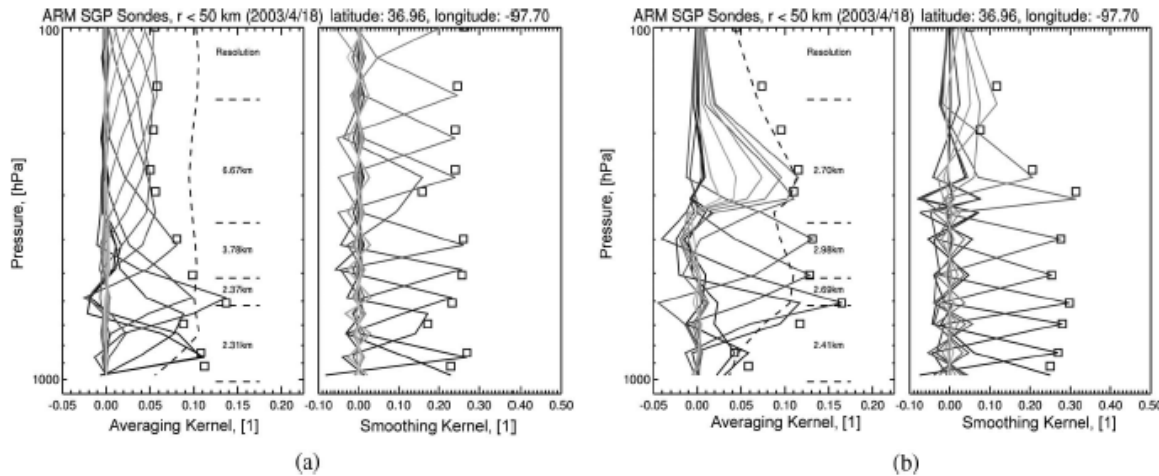


Fig. 4. Example of effective averaging kernels  $\mathbf{F}\Phi\mathbf{F}^+$  and smoothing kernels  $\mathbf{F}\mathbf{F}^+$  for a midlatitude case over the ARM site SGP on April 23, 2003.

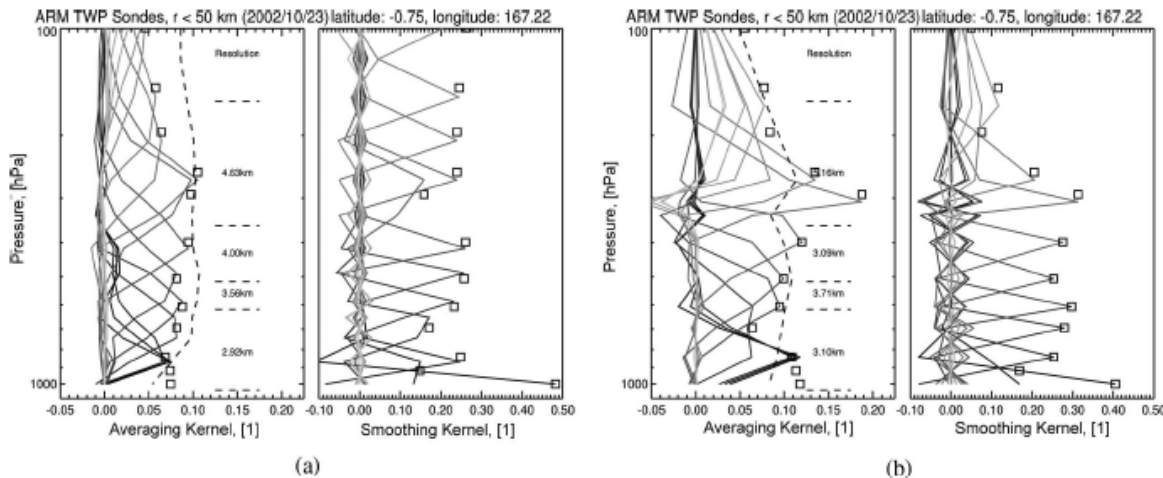


Fig. 5. Example of effective averaging kernels  $\mathbf{F}\Phi\mathbf{F}^+$  and smoothing kernels  $\mathbf{F}\mathbf{F}^+$  for a tropical case over the ARM site TWP on October 23, 2002.

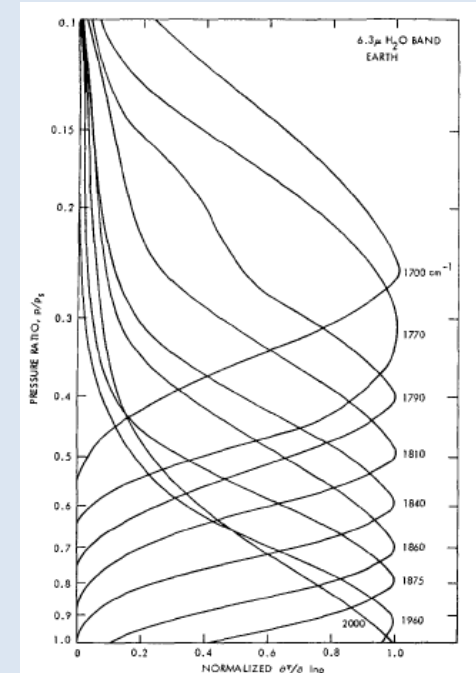


FIG. 1. Normalized weighting functions ( $d\tau/d \ln p$ ) for the selected set of nine sounding frequencies computed for an instrumental slit function of  $5 \text{ cm}^{-1}$  (see text).

Compare weighting functions

From: Maddy and Barnett (2008), Vertical resolution estimates in version 5 of AIRS operational retrievals, TGARS.

## Finally: The Null Space

- The set of *unobservable states*. Examples:
  - Vertical structure smaller than averaging kernel scales.
  - Scenes obscured by clouds (infrared) or precipitation (microwave).

*Understanding the null space is a fundamental challenge of atmospheric remote sensing. Auxiliary information is needed to define it.*

# Some Thoughts on the Future

- *Interpretation of retrieved quantities remains a challenge*
  - Though less daunting than observed (cloudy) radiances.
  - We have a lot of both radiances and retrievals.
- *Retrieval methodologies are still relatively immature*
  - Statistical and relaxation methods are near their limit of usefulness for characterizing errors.
  - Optimal estimation methods have not been widely applied to the very large data sets from NASA facility instruments (MODIS and AIRS).
  - *Retrieving cloud state with other properties is the main challenge.*
- *Model assimilation of cloud-affected radiances for  $T$  and  $q$  is a BIG challenge.*

# References

- **Books:**

- Good intro: Menke, 1989, Geophysical Data Analysis: Discrete Inverse Theory, Academic, New York.
- General theory: R. L. Parker, 1994, Geophysical Inverse Theory, Princeton
- Theoretical with atmospheric emphasis: C. D. Rodger, 2000, Inverse Methods for Atmospheres: Theory and Practice, World Scientific, 2008 reprinting.
- Intro and instrumentation: S. Kidder and T. Vonder Haar, 1994, Satellite Meteorology: An Introduction, Academic Press.

- **Papers:**

- Chahine, M. T., 1970, J. Atmos. Sci.
- Smith, W., 1970, Applied Optics.
- Worden et al., 2004, JGR.
- Maddy and Barnet, 2008, TGARS.
- Gordley and Russel, Appl. Optics, 1981.

# Supplementary Slides

# Spectral Bands Determined by Radiative Transfer Physics *and Technology*

- Visible
  - Very high horizontal resolution.
  - Low atmospheric opacities => applicable to aerosol, clouds and surface.
  - Calibration to better than 10% is difficult.
- Infrared
  - Moderate horizontal resolution (~10 km; higher possible).
  - High spectral resolution.
  - Can be calibrated to ~0.1 K RMSE brightness temperature.
  - Mixed atmospheric opacities => information about vertical structure, clouds, and surface.
  - Cannot sound through cloud optical depths  $\geq 1$ .

# Spectral Bands Determined by Radiative Transfer Physics and Technology (continued)

- Microwave
  - Mixed atmospheric opacities (like infrared).
  - Small cloud opacities
    - Can sound into non-precipitating clouds.
  - Lower spectral and spatial resolution because of receiver and antenna costs
    - Limited spectral resolution translates to limited vertical information.

Note: Resolution and sensitivity for all wavelengths are closely tied to the *observational null space*.